

X_1	X_2
2	3
5	4
0	5
-3	0

By using Manhattan distance and the initial cluster centers given below, find new position of the cluster centers after the first iteration. Consider as $c_1=(0, 1)$ and $c_2=(5, 5)$.

$$\begin{aligned}
 d_{1c_1} &= |0-2| + |1-3| = 4 & d_{1c_2} &= |5-2| + |5-3| = 5 & \text{(the first sample belongs to } c_1) \\
 d_{2c_1} &= |0-5| + |1-4| = 8 & d_{2c_2} &= |5-5| + |5-4| = 1 & \text{(the second sample belongs to } c_2) \\
 d_{3c_1} &= |0-0| + |1-5| = 4 & d_{3c_2} &= |5-0| + |5-5| = 5 & \text{(the third sample belongs to } c_1) \\
 d_{4c_1} &= |0-(-3)| + |1-0| = 4 & d_{4c_2} &= |5-(-3)| + |5-0| = 13 & \text{(the fourth sample belongs to } c_1)
 \end{aligned}$$

according to data points, we can update the cluster centers

$$c_1 = \text{mean}(x_i \text{ belongs to } c_1) = (-1/3, 8/3)$$

$$c_2 = (5, 4)$$

X_1	X_2	D
2	3	A
5	4	B
0	5	A
-3	0	B

By using Manhattan distance and $K=1$, find the class of $(-2, 2)$

$$\begin{aligned}
 d_1 &= |-2-2| + |2-3| = 5 & d_2 &= |-2-5| + |2-4| = 9 & d_3 &= |-2-0| + |2-5| = 5 \\
 d_4 &= |-2+3| + |2-0| = 3
 \end{aligned}$$

because the nearest one point is fourth data point, its class is B

for $K=3$, find the class of $(-2, 2)$

We found the nearest three data points in dataset are x_1, x_3, x_4 . Among (A,A,B) classes we have to choose "A" as major

for $K=3$, find the class of $(5, 3)$

Because the nearest three points are the first three data points, its class is A.