

X ₁	X ₂	D
2	3	1
5	4	0
1	5	1

By using perceptron (single neuron) method, find the weights of neuron model after the first iteration only. (Note: we can accept the initial values of all weights (also theta) as zero, and learning rate is 0.5)

$w_1=0$
 $w_2=0$
 $b=0$
 $Q=0$
 $\eta=0.5$

compute net1 (for the first sample 2,3:1)

$$\text{net}_1 = 2*0 + 3*0 + 0 = 0$$

$y_1 = 0$ but since $d_1=1$ $e_1=d_1-y_1=1$

$$Dw_1 = 0.5*1*2 = 1 \rightarrow w_1 = w_1 + Dw_1 = 0 + 1 = 1$$

$$Dw_2 = 0.5*1*3 = 1.5 \rightarrow w_2 = w_2 + Dw_2 = 0 + 1.5 = 1.5$$

$$Db = 0.5*1 = 0.5 \rightarrow b = b + Db = 0 + 0.5 = 0.5$$

compute net2 (for the second sample 5,4:0)

$$\text{net}_2 = 5*1 + 4*1.5 + 0.5 = 11.5$$

$y_2 = 1$ but since $d_2=0$ $e_2=d_2-y_2=-1$

$$Dw_1 = 0.5*(-1)*5 = -2.5 \rightarrow w_1 = w_1 + Dw_1 = 1 - 2.5 = -1.5$$

$$Dw_2 = 0.5*(-1)*4 = -2 \rightarrow w_2 = w_2 + Dw_2 = 1.5 - 2 = -0.5$$

$$Db = 0.5*(-1) = -0.5 \rightarrow b = b + Db = 0.5 - 0.5 = 0$$

compute net3 (for the third sample 1,5:1)

$$\text{net}_3 = 1*-1.5 + 5*-0.5 + 0 = -4$$

$y_3 = 0$ but since $d_3=1$ $e_3=d_3-y_3=1$

$$Dw_1 = 0.5*1*1 = 0.5 \rightarrow w_1 = w_1 + Dw_1 = -1.5 + 0.5 = -1$$

$$Dw_2 = 0.5*1*5 = 2.5 \rightarrow w_2 = w_2 + Dw_2 = -0.5 + 2.5 = 2$$

$$Db = 0.5*1 = 0.5 \rightarrow b = b + Db = 0 + 0.5 = 0.5$$

$w_1=-1$ $w_2=2$ $b=0.5$

In order to find MSE,

compute net1 (for the first sample 2,3:1)

$$\text{net}_1 = 2*w_1 + 3*w_2 + b = 4.5 \quad y_1 = 1 \quad \text{since } d_1=1 \quad e_1=d_1-y_1=0$$

compute net2 (for the second sample 5,4:0)

$$\text{net}_2 = 5*w_1 + 4*w_2 + b = 3.5 \quad y_2 = 1 \quad \text{since } d_2=0 \quad e_2=d_2-y_2=-1$$

compute net3 (for the third sample 1,5:1)

$$\text{net}_3 = 1*w_1 + 5*w_2 + b = 9.5 \quad y_3 = 1 \quad \text{since } d_3=1 \quad e_3=d_3-y_3=0$$

$$\text{MSE} = (0^2 + (-1)^2 + 0^2) / 3 = 0.33$$

By using adaline (single neuron) method, find the weights of neuron model after the first iteration only. (Note: we can accept the initial values of all weights (also theta) as zero, and learning rate is 0.5)

$w_1=1$
 $w_2=-1$
 $b=0$
 $\eta=0.5$

compute net1 (for the first sample 2,3:1)

$$\text{net}_1 = 2 \cdot 1 + 3 \cdot (-1) + 0 = -1$$

$$y_1 = 0 \text{ since } d_1 = 1 \quad e_1 = d_1 - \text{net}_1 = 1 - (-1) = 2$$

$$Dw_1 = 0.5 \cdot 2 \cdot 2 = 2 \rightarrow w_1 = w_1 + Dw_1 = 1 + 2 = 3$$

$$Dw_2 = 0.5 \cdot 2 \cdot 3 = 3 \rightarrow w_2 = -1 + 3 = 2$$

$$Db = 0.5 \cdot 2 = 1 \rightarrow b = 0 + 1 = 1$$

compute net2 (for the second sample 5,4:0)

$$\text{net}_2 = 5 \cdot 3 + 4 \cdot 2 + 1 = 24$$

$$y_2 = 1 \text{ but since } d_2 = 0 \quad e_2 = d_2 - \text{net}_2 = 0 - 24 = -24$$

$$Dw_1 = 0.5 \cdot (-24) \cdot 5 = -60 \rightarrow w_1 = 3 - 60 = -57$$

$$Dw_2 = 0.5 \cdot (-24) \cdot 4 = -48 \rightarrow w_2 = 2 - 48 = -46$$

$$Db = 0.5 \cdot (-24) = -12 \rightarrow b = 1 - 12 = -11$$

compute net3 (for the third sample 1,5:1)

$$\text{net}_3 = 1 \cdot (-57) + 5 \cdot (-46) - 11 = -298$$

$$y_3 = 0 \text{ since } d_3 = 1 \quad e_3 = d_3 - \text{net}_3 = 1 - 298 = -297$$

$$Dw_1 = 0.5 \cdot (-297) \cdot 1 = -148.5 \rightarrow w_1 = -57 - 148.5 = -205.5$$

$$Dw_2 = 0.5 \cdot (-297) \cdot 5 = -742.5 \rightarrow w_2 = -46 - 742.5 = -788.5$$

$$Db = 0.5 \cdot (-297) = -148.5 \rightarrow b = -11 - 148.5 = -159.5$$

$$w_1 = -205.5 \quad w_2 = -788.5 \quad b = -159.5$$